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**Supporting Online Material**  
[www.sciencemag.org/cgi/content/full/1088876/DC1](http://www.sciencemag.org/cgi/content/full/1088876/DC1)  
 Materials and Methods  
 Figs. S1 to S3

7 July 2003; accepted 11 August 2003  
 Published online 21 August 2003;  
 10.1126/science.1088876  
 Include this information when citing this paper.

## Cooling Bose-Einstein Condensates Below 500 Picokelvin

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Spin-polarized gaseous Bose-Einstein condensates were confined by a combination of gravitational and magnetic forces. The partially condensed atomic vapors were adiabatically decompressed by weakening the gravito-magnetic trap to a mean frequency of 1 hertz, then evaporatively reduced in size to 2500 atoms. This lowered the peak condensate density to  $5 \times 10^{10}$  atoms per cubic centimeter and cooled the entire cloud in all three dimensions to a kinetic temperature of  $450 \pm 80$  picokelvin. Such spin-polarized, dilute, and ultracold gases are important for spectroscopy, metrology, and atom optics.

The pursuit of lower temperatures is motivated by the quest to observe phenomena that occur on very low energy scales, in particular, phase transitions to new forms of matter. The achievement of temperatures near 1 K in solids and in liquids led to the discoveries of superconductivity (1) and superfluidity (2), respectively. The advent of laser cooling resulted in microkelvin temperature atomic vapors (3–5), subsequently cooled to nanokelvin temperatures by evaporative cooling to form dilute Bose-Einstein condensates (6, 7) and quantum degenerate Fermi gases (8). Collectively, these low-temperature systems have a host of applications, including superconducting quantum interference devices (SQUIDs) (9), superfluid gyroscopes (10, 11), and atomic clocks (12).

Temperature is a quantity that parameterizes how energy is distributed across the available states of a system, and effective temperatures can be defined for decoupled degrees of freedom or subsets of particles. For example, nuclear spins isolated from the

kinetic motion of their respective atoms have been cooled by adiabatic demagnetization to an effective temperature of 280 pK (13). Spin ensembles have a finite number of available states, such that a spin-polarized sample, as in our work, would be characterized by zero effective temperature. In contrast, the motion of free particles is subject to a continuum of states, and the kinetic temperature of an ensemble can only asymptotically approach absolute zero.

Effective temperatures in atomic vapors are defined by the widths of velocity distributions, which can be much smaller than the mean velocity of the sample. Raman cooling (14, 15) and velocity-selective coherent population trapping (VSCPT) (16) have generated velocity distributions with very narrow peaks, corresponding to nanokelvin and picokelvin effective temperatures. However, these temperatures were associated with the motion of only a subset of the atoms in the cloud and/or with atomic motion in only one dimension.

For trapped, partially condensed atomic vapors, the condensate fraction has zero entropy and the kinetic temperature of the sample is determined by the velocity distribution of the thermal (noncondensed) component. When released, the condensate fraction expands more slowly than the thermal compo-

nent and has been characterized by picokelvin effective temperatures for anisotropic (17) and noninteracting (18) gases.

Cooling the atomic motion of entire ensembles in all three dimensions has proven difficult. To date, kinetic temperatures of a few hundred nanokelvin have been achieved with adiabatic and optical cooling (19, 20), and evaporative cooling techniques have produced condensates with temperatures of 3 nK (21). By adiabatic expansion and subsequent evaporation, we have cooled partially condensed atomic vapors to picokelvin kinetic temperatures.

Our thermometry is calibrated by the Bose-Einstein condensation (BEC) phase transition temperature,  $T_c$ , which in the thermodynamic limit for a harmonically trapped ideal Bose gas is (22)

$$k_B T_c = \hbar \bar{\omega} \left( \frac{N}{\zeta(3)} \right)^{1/3} \approx 0.94 \hbar \bar{\omega} N^{1/3} \quad (1)$$

where  $k_B$  is Boltzmann's constant,  $\hbar$  is Planck's constant  $h$  divided by  $2\pi$ ,  $\zeta(n)$  is the Riemann Zeta function,  $\bar{\omega} = (\omega_x \omega_y \omega_z)^{1/3}$  is the geometric mean of the harmonic trap frequencies, and  $N$  is the total number of atoms, both condensed and noncondensed. Thus, the atom number and the trap frequencies set an upper limit for the temperature of a confined Bose-Einstein condensate. In our work, adiabatically weakening the trapping potential to a mean frequency of  $\bar{\omega} = 2\pi \times (1.12 \pm 0.08)$  Hz guaranteed that partially condensed atomic vapors with  $N \leq 8000$  atoms had picokelvin temperatures ( $T_c \leq 1$  nK).

Bose-Einstein condensates containing more than  $10^7$   $^{23}\text{Na}$  atoms were created in the weak field seeking  $|F = 1, m_F = -1\rangle$  state in a magnetic trap, captured in the focus of an optical tweezers laser beam, and transferred into an auxiliary "science" chamber as described in (23). In the science chamber, condensates containing  $2 \times 10^6$  to  $3 \times 10^6$  atoms were transferred from the optical tweezers into a gravito-magnetic trap (Fig. 1A). A small coil carrying current  $I_S$  generated a vertical bias field  $B_z$  and supported the condensates against gravity with a vertical magnetic field gradient,  $B'_z = 2$  mg/

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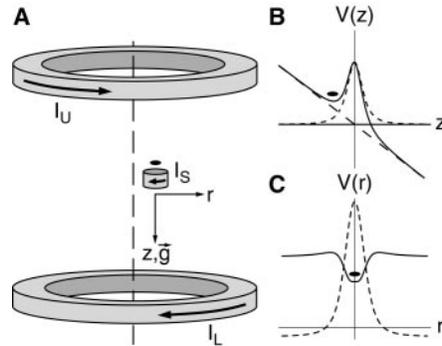
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$\mu_B \approx 8$  G/cm, where  $m$  is the atomic mass,  $g$  is the gravitational acceleration, and  $\mu_B$  is the Bohr magneton. Additional control over  $B_z$  and  $B'_z$  was provided by two external coils carrying independent currents  $I_U$  and  $I_L$ . Weak curvature,  $B'_z$ , to the vertical bias field created stable vertical confinement such that a harmonic restoring force was provided magnetically (gravitationally) for downward (upward) vertical displacements (Fig. 1B). A radial field gradient,  $B'_r = \partial B_z / \partial r = -B'_z/2$ , was also present and added in quadrature with  $B_z$  to provide harmonic radial confinement with a restoring force proportional to  $(B'_z)^2/B_z$  (Fig. 1C). The trapping potential does not have fundamental radial asymmetries as do previously demonstrated Ioffe-Pritchard magnetic traps (17, 24, 25). In principle, stable three-dimensional confinement is possible above a single coil in the presence of gravity without the aid of external bias fields or gradients.

For typical loading parameters— $I_S = 340$  mA,  $I_U = 5.5$  A, and  $I_L = 0$ —the gravito-magnetic trap was spherically symmetric, with trap frequencies  $\omega_x \approx \omega_y \approx \omega_z \approx 2\pi \times 8$  Hz. Condensates loaded into the gravito-magnetic trap from the optical tweezers were held for 5 s to allow for the damping of excitations. The resulting partially condensed clouds had  $\sim 5 \times 10^5$  atoms and a BEC transition temperature  $T_c = 30$  nK. Throughout our work, the atomic vapor maintained a temperature  $T$  such that  $0.5 < TT_c < 1$ .

Further cooling was accomplished by adiabatically decompressing the trapping potential in two 5 s stages, with a 5 s delay in between to allow excitations to damp. In the first stage, the vertical frequency was reduced to  $\omega_z = 2\pi \times (1.81 \pm 0.05)$  Hz by simultaneously raising currents  $I_L$  and  $I_U$  by identical amounts and lowering the current  $I_S$  by a factor of 10. This transferred the dominant source of magnetic field gradient from the small coil to the external coils, with the remaining vertical curvature still due to the reduced  $I_S$ . In the second stage, the radial frequencies were reduced to  $\omega_x = 2\pi \times (0.65 \pm 0.05)$  Hz and  $\omega_y = 2\pi \times (1.2 \pm 0.1)$  Hz by raising  $I_L$  and lowering  $I_U$  by identical amounts. The vertical magnetic field gradient and curvature remained constant, but the vertical bias field,  $B_z$ , increased. This reduced the radial confinement due to the scaling  $\omega_r \propto B'_r / B_z^{1/2}$  (24, 25).

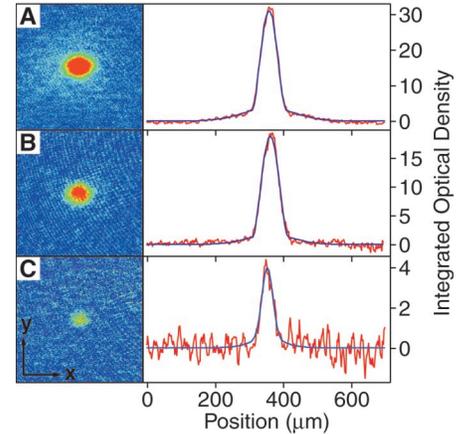
For currents  $I_S = 34$  mA,  $I_U = 14$  A, and  $I_L = 44$  A, the final gravito-magnetic trap had a measured mean frequency  $\bar{\omega} = 2\pi \times (1.12 \pm 0.08)$  Hz and axial bias field  $B_z = 17$  G. The residual anharmonicities of the trapping potential were small, with  $\Delta\omega/\omega = 0.1$  for 500  $\mu\text{m}$  displacements from the trap center. Further radial decompression was not possible because of a finite trap depth (Fig. 1C) and sensitivity of trap stability to milli-gauss level radial bias fields.



**Fig. 1.** Gravito-magnetic trap. (A) Bose-Einstein condensates were levitated against gravity  $\sim 5$  mm above a 1-cm diameter, 25-turn coil mounted inside the ultrahigh vacuum chamber running current  $I_S$ . Two 10-cm diameter, 20-turn coils were mounted outside the vacuum chamber and were supplied individually with currents  $I_U$  and  $I_L$ . The vertical separation between the large coils was 10 cm. The 1-cm diameter coil was mounted radially off-axis with respect to the pair of 10-cm diameter coils by  $\sim 1$  cm. This broke the cylindrical symmetry of the trapping potential. Additional bias fields of  $\sim 1$  G were applied in the horizontal plane to cancel the radial magnetic fields generated by  $I_U$  and  $I_L$  on the axis of the small coil and to maintain a stable trapping potential.  $\vec{g}$  denotes the direction of gravitational acceleration. (B) Magnetic potential due to  $I_S$  (short dashed line), gravitation potential (long dashed line), and joint vertical potential of the gravito-magnetic trap (solid line). (C) A radially repulsive potential magnetic potential was generated by running  $I_S$  alone (dashed line); however, applying a slight antibias field with  $I_U$  modified the radial energy profile and created a magnetic field minimum at  $r = 0$  (solid line). In (A) to (C), the solid oval denotes the trapped condensate.

After decompression, the partially condensed atomic vapors had  $\sim 2 \times 10^5$  atoms and a BEC transition temperature  $T_c = 3$  nK.  $T_c$  was lowered further by reducing the number of atoms in the cloud (Eq. 1), while maintaining a substantial condensate fraction at all times ( $0.5 < TT_c < 1$ ). The atom number was reduced by holding the atoms in the gravito-magnetic trap for up to 200 s. Often, microwave radiation near the  $|1, -1\rangle \rightarrow |2, 0\rangle$  transition was applied to shorten the hold time required to arrive at lower atom number to 10 s. The atom number reduction was accompanied by cooling, during which the elastic collision rate (between thermal atoms and the condensate) dropped from 0.25 Hz to 0.01 Hz. Therefore, a few collisions were sufficient to cause evaporation out of the finite depth trap. This cooling was not efficient in the sense of providing a gain in phase-space density but still was capable of maintaining thermal equilibrium and lowering the absolute temperature of the vapor.

Using this technique, we cooled partially condensed vapors containing up to 30,000 atoms to temperatures below 1 nK (Figs. 2 and 3). Our lowest measured three-

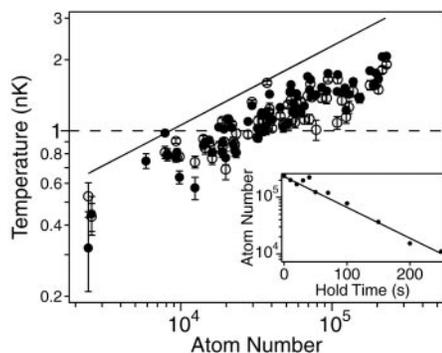


**Fig. 2.** Picokelvin temperature thermometry. Partially condensed atomic vapors confined in the gravito-magnetic trap with (A) 28,000, (B) 16,000, and (C) 2,500 atoms. The one-dimensional cross sections (red) were obtained by integrating the two-dimensional absorption images of the trapped clouds along the  $y$  axis. Bimodal fits to Eq. 2 (blue) yielded temperatures of (A)  $1.05 \pm 0.08$  nK, (B)  $780 \pm 50$  pK, and (C)  $450 \pm 80$  pK, where the uncertainty is due to the fit of an individual image. The absorption imaging light was resonant with the  $F = 2 \rightarrow F' = 3$  cycling transition for the trapped atoms and was aligned with the vertical ( $z$ ) axis. The atoms were optically pumped into the  $F = 2$  hyperfine level with a pulse resonant with the  $F = 1 \rightarrow F' = 2$  transition. The field of view for the absorption images in (A) to (C) is  $460 \mu\text{m} \times 460 \mu\text{m}$ .

dimensional kinetic temperature was  $450 \pm 80$  pK for 2500 atoms at a peak condensate density of  $5 \times 10^{10}$  atoms/cm<sup>3</sup>. Under these conditions, the peak atom-atom interaction energy was  $\mu = k_B \times 33$  pK, while the zero point energy of the harmonic trapping potential was  $(1/2)\hbar \bar{\omega} \approx k_B \times 24$  pK. Condensates released from the gravito-magnetic trap would expand with energies of this order and therefore could be characterized by effective temperatures  $\sim 30$  pK.

Additional cooling would require lowering the trap frequencies further or reducing the atom number more. However, weakly confining traps have proven technically difficult to control such that lowering  $\bar{\omega}/2\pi$  substantially below 1 Hz is challenging. Likewise, because  $T_c \propto N^{1/3}$ , atom number reduction by an order of magnitude only results in temperature reduction by a factor of two. Furthermore, lower temperatures and lower densities are accompanied by collisional equilibrium times approaching 100 s.

Because  $\mu \approx \hbar\bar{\omega}$ , the condensates in the gravito-magnetic trap were in a density regime intermediate between the Thomas-Fermi ( $\mu \gg \hbar\bar{\omega}$ ) and ideal ( $\mu \ll \hbar\bar{\omega}$ ) gas limits. No simple approximation describes the condensate wave function, but the number of thermal atoms,  $N_{\text{th}} = \zeta(3) \times (k_B T / \hbar\bar{\omega})^3$ , and the width of their distribution,



**Fig. 3.** Bose-Einstein condensates at picokelvin temperatures. The temperature of more than 60 partially condensed atomic vapors is plotted versus total number of condensed and noncondensed atoms. A solid line at the Bose-Einstein condensation phase transition temperature (Eq. 1) and a dashed line at 1 nK are provided as guides. Condensate temperatures were determined from one-dimensional fits to atomic density cross sections integrated along either the  $x$  (closed circles) or  $y$  (open circles) axis (Fig. 2). Differences in the two measured temperatures for a single condensate reflect the true uncertainty of the measurement. Plotted error bars represent the statistical uncertainty of the fit. The inset shows that the  $1/e$  condensate lifetime in the gravito-magnetic trap was limited by one-body processes to  $80 \pm 5$  s.

$w_{\text{th}} = (2k_B T / m\omega^2)^{1/2}$ , in any spatial direction can be related to the temperature, provided that the thermal energy is much larger than the trap level spacing,  $k_B T \gg \hbar \bar{\omega}$ , where  $\omega$  is the trap frequency for the axis along which  $w_{\text{th}}$  is measured (22). The ratio of atoms in the condensate,  $N_0$ , to the total number of atoms,  $N = N_0 + N_{\text{th}}$ , is also related to the temperature through  $N_0/N = 1 - (T/T_c)^3$ .  $N_0$ ,  $N_{\text{th}}$ , and  $w_{\text{th}}$  are therefore completely determined by  $T$  and  $N$ .

The temperature of the atomic vapors was extracted by fitting integrated, one-dimensional atomic density cross sections to a bimodal distribution (Fig. 2)

$$n(x) = N_0 \Psi_0^2 + \frac{N_{\text{th}}}{\sqrt{\pi} w_{\text{th}}} e^{-x^2/w_{\text{th}}^2} \quad (2)$$

where  $\Psi_0^2$  is a bell-shaped function with width  $w_0$  that describes the condensate peak [ $\Psi_0^2 = (15/16) w_0^{-1} \max(1 - x^2/w_0^2, 0)^2$  for a Thomas-Fermi gas and  $\Psi_0^2 = w_0^{-1} \pi^{-1/2} \exp(-x^2/w_0^2)$  for an ideal gas]. The fitted parameters were  $T$ ,  $N$ , and  $w_0$ . We checked that the fitted temperature did not depend on the exact choice of the condensate wave function (inverted parabola or gaussian) or the application of microwave radiation to reduce atom number.

All atomic vapors represented in Fig. 3 had a clear bimodal density distribution from which a temperature was reproducibly extracted. The temperatures extracted from one-dimensional fits along both radial axes were nominally the same, empirically indicating

that the atomic vapors remained close to thermal equilibrium at all times.

In conclusion, we have created long-lived ( $80 \pm 5$  s), low-temperature ( $450 \pm 80$  pK), and low-density ( $5 \times 10^{10}$  atoms/cm<sup>3</sup>) partially condensed atomic vapors using a weakly confining [ $\bar{\omega} = 2\pi \times (1.12 \pm 0.08)$  Hz] gravito-magnetic trap. These samples are characterized by a thermal velocity  $\sim 1$  mm/s, a speed of sound  $\sim 100$   $\mu$ m/s, and a healing length limited by the  $\sim 20$ - $\mu$ m harmonic oscillator length of the trapping potential. Low-temperature and low-density ensembles are important for spectroscopy, metrology, and atom optics. In addition, they are predicted to experience quantum reflection from material surfaces (26–28).

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- This work was funded by the Army Research Office, NSF, Office of Naval Research, and NASA. We thank C. V. Nielsen for experimental assistance and J. K. Thompson for critical comments on the manuscript. M.S. acknowledges additional support from the Swiss National Science Foundation.

7 July 2003; accepted 12 August 2003

## Observation of Polymer Conformation Hysteresis in Extensional Flow

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Highly extensible *Escherichia coli* DNA molecules in planar extensional flow were visualized in dilute solution by fluorescence microscopy. For a narrow range of flow strengths, the molecules were found in either a coiled or highly extended conformation, depending on the deformation history of the polymer. This conformation hysteresis persists for many polymer relaxation times and is due to conformation-dependent hydrodynamic forces. Polymer conformational free-energy landscapes were calculated from computer simulations and show two free-energy minima for flow strengths near the coil-stretch transition. Hysteresis cycles may directly influence bulk-solution stresses and the development of stress-strain relations for dilute polymer flows.

The behavior of long-chain, flexible polymer molecules in extension-dominated flows has been the subject of research discussion for more than 30 years (1). Flows of dilute poly-

mer solutions exhibit several interesting macroscopic effects including flow-dependent viscosity, enhanced normal stresses, and turbulent-drag reduction. Such non-Newtonian fluid properties result from flow-induced changes in the polymer conformations in solution. In short, a flowing fluid will influence polymer configurations in solution, and the forces exerted back on the fluid are directly related to the molecular conformations.

Polymer conformations and the resultant bulk-solution stresses are affected by flow type. In general, flows with a large rotational

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