

# Exercises

1. Use the definition of field quadratures  $X_1(t)$  and  $X_2(t)$  to verify what are their physical dimensions.
2. A ruby laser operating at 693nm emits pulses of energy 1mJ. Calculate the uncertainty in the phase of the laser light .
3. The proposed Laser Interferometer Space Antenna (LISA) experiment for gravity wave detection will use a standard Michelson interferometer (i.e. no power recycling or cavity enhancement) with a laser operating at 1064 nm. The length of the arms of the interferometer is  $5 \times 10^6$  km and the power of the beams that form the interference pattern is  $\sim 10^{-11}$  W. Calculate the minimum strain that can be detected.
4. !! Demonstrate that an elastic force  $F = -kx(1 - \varepsilon \sin 2\omega_0 t)$  modulated at twice the natural frequency ( $\varepsilon \ll 1$ ) produces on an object of mass  $m$  oscillations that grow in time at one quadrature, while are damped at the other quadrature.